The Model

Positive Interest Rates

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Fiscal Consequences of Paying Interest on Reserves

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Interest on Reserves in the U.S.

- Introduced as a minor tweak to remove an implicit tax on banks
- Not present at the beginning of QE1, replaced coordinated action with Treasury



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Interest on Reserves in the U.S.

- Introduced as a minor tweak to remove an implicit tax on banks
- Not present at the beginning of QE1, replaced coordinated action with Treasury
- Resulted in an underappreciated enormous expansion of Fed fiscal powers



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Plan of the Talk

- Lay our textbook environment of interaction between Treasury, CB
- Illustrate public finance implications of different CB strategies
- Match CB strategies with alternative Treasury strategies that would yield same fiscal risk



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Plan of the Talk

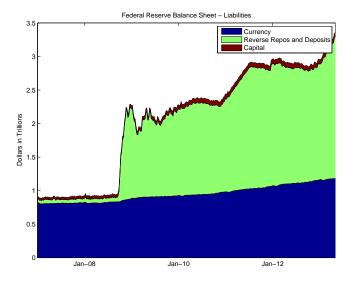
- Lay our textbook environment of interaction between Treasury, CB
- Illustrate public finance implications of different CB strategies
- Match CB strategies with alternative Treasury strategies that would yield same fiscal risk
- Ultimate question: if alternative Treasury strategies are possible, who should decide fiscal risk?





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Fed Liabilities since 2007



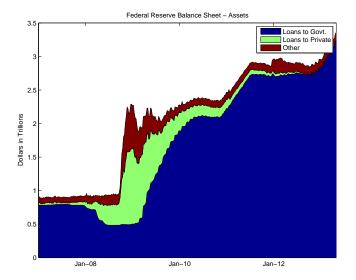
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Fed Assets since 2007

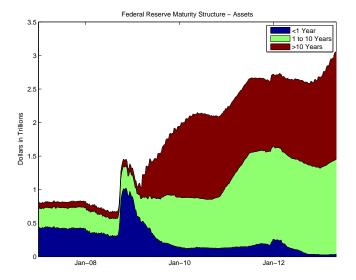


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Fed Maturity Structure of Assets since 2007



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Interest on Reserves at the ECB and B of E

- Always part of their powers
- Not used by B of E before QE
- Deposits were nontrivial at the ECB, grew after 2008



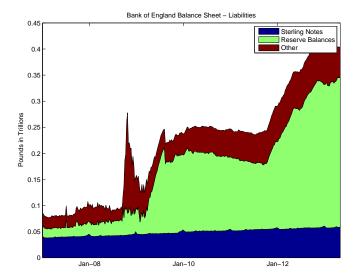


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Bank of England Liabilities since 2007

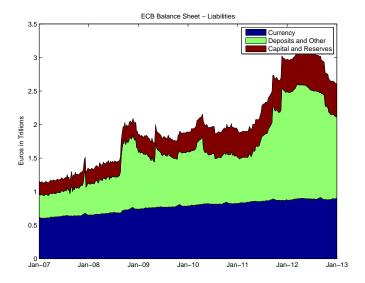






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ECB Liabilities since 2007



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The Model: Agents

- Households (identical)
- Treasury
- Central Bank
- Households: maximizers, Treasury and CB: automata



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- Goods produced with labor, CRS technology, productivity 1
- Cash-in-advance on all goods (leisure is credit good)



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Preferences

$$E_0 \sum_{t=0}^{\infty} \left(\prod_{s=0}^{t-1} \beta_s \right) \left[u(c_t) - \phi y_t \right]$$

Discount rate shock: only shock in the economy



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Traded Assets

- One-period securities issued by Treasury: B_t (B_t^B held by CB), interest rate R_t
- Consols issued by Treasury: D_t (D_t^B held by CB), price Q_t
- Money (cash, used for CIA): M_t
- One-period reserves at the CB: X_t, must pay R_t if positive



Equilibrium Conditions from Private Optimization

- Money demand: $M_t/P_t = L(R_t)$
- Fisher relation (Euler equation): $1 = \beta_t E_t[(1 + R_{t+1})P_t/P_{t+1}]$
- Ex-dividend price of consols:

$$Q_t = rac{1}{1+R_t} \left[1+eta_t E_t \left(rac{(1+R_{t+1})P_t}{P_{t+1}} Q_{t+1}
ight)
ight]$$

• (Nominal) asset pricing kernel:

$$z_t = \frac{1 + R_t}{1 + R_0} \frac{P_0}{P_t} \prod_{s=0}^{t-1} \beta_s$$

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Budget Constraints in Flows

• Treasury:

$$B_{t-1} + D_{t-1} = \frac{B_t}{1+R_t} + Q_t(D_t - D_{t-1}) + S_t + T_t$$

• CB:

$$M_t - M_{t-1} = \frac{B_t^B}{1 + R_t} - B_{t-1}^B + Q_t (D_t^B - D_{t-1}^B) - D_{t-1}^B + S_t - \frac{X_t}{1 + R_t} + X_{t-1}$$



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Budget Constraints, Present-Value Form

• Treasury:

$$B_{t-1} + (1+Q_t)D_{t-1} = \frac{1}{z_t}E_t\sum_{s=t}^{\infty} z_s(S_s+T_s)$$

$$B_{t-1}^{B} + (1+Q_t)D_{t-1}^{B} - X_{t-1} - M_{t-1} + \frac{1}{z_t}E_t\sum_{s=t}^{\infty} z_s\left(M_s\frac{R_s}{1+R_s}\right) =$$

$$\frac{1}{z_t}E_t\sum_{s=t}^{\infty}z_sS_s$$



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Ricardian Equivalence, Modigliani-Miller

- Ricardian equivalence holds (within the spanned set)
- Modigliani-Miller for CB: given CE, construct a new CE by:
 - Increase S_{t_1} by ΔS
 - Decrease B_s between t_1 and t_2 by $\Delta S \prod_{\nu=t_1}^{s} (1+R_{\nu})$
 - Decrease CB holdings B_s^B by same amount, or increase X_s by same amount
 - Decrease S_{t_2} by $\Delta S \prod_{\nu=t_1}^{t_2-1} (1+R_{\nu})$



Does CB Dividend Policy Matter?

- Modigliani-Miller says timing of dividend payments does not matter
- But it may matter for decisions taken over time when conflict is present. Example:

$$S_0 > B_{-1}^B + (1+Q_0)D_{-1}^B - X_{-1} - M_{-1} + \sum_{s=0}^{\infty} \text{PV}_0\left(M_s \frac{R_s}{1+R_s}\right)$$

Then CB starts period 1 with net liabilities greater than future profits, needs a transfer from Treasury.

• Timing may not matter, PV of seigniorage payments (and risk profile) does matter



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Accounting for CB profits

• At historical cost:

$$\Pi_t^{HC} := \frac{R_{t-1}}{1 + R_{t-1}} (B_{t-1} - X_{t-1}) + D_{t-1}^B + (Q_t - \bar{Q}_{t-1}) (D_{t-1}^B - D_t^B) I_{D_{t-1}^B > D_t^B},$$

• Marked to market:

$$\Pi_t^{MM} := \frac{R_{t-1}}{1+R_{t-1}} (B_{t-1} - X_{t-1}) + D_{t-1}^B + (Q_t - Q_{t-1}) D_{t-1}^B$$

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Roadmap

- Sequence of CB strategies
- Increasingly aggressive
- Review implications for CB profits

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1. Bills Only

Strategy:

- No interest on reserves $(X_t = 0)$;
- All CB assets invested in short-term debt ($D_t = 0$). Implications:

•

$$\Pi_t^{HC} = \Pi_t^{MM} = \frac{R_t}{1+R_t} B_t^B \ge 0$$

Inequalities strict, unless CB holds no assets (pure fiat money)

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2. Hold to Maturity

Strategy:

- No interest on reserves $(X_t = 0)$;
- Consols are never sold $(D_t \ge D_{t-1})$.

Implications:

$$\Pi_t^{HC} = \frac{R_{t-1}}{1 + R_{t-1}} B_{t-1} + D_{t-1}^B \ge 0$$

$$\Pi_t^{MM} := \frac{R_{t-1}}{1+R_{t-1}} (B_{t-1} - X_{t-1}) + D_{t-1}^B + (Q_t - Q_{t-1}) D_{t-1}^B$$

Could turn negative, but within bounds (more to come)

3. Active Trading, but no Interest on Reserves

Strategy:

- No interest on reserves $(X_t = 0)$;
- Consols are bought and sold (but no short sales of any government debt)

Implications:

• Even Π_t^{HC} can turn negative when capital losses are realized:

$$\Pi_t^{HC} := \frac{R_{t-1}}{1+R_{t-1}} B_{t-1} + D_{t-1}^B + (Q_t - \bar{Q}_{t-1})(D_{t-1}^B - D_t^B) I_{D_{t-1}^B > D_t^B},$$

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A Special Case: Pure Fiat Money

• Assume that $M_t \ge M_{t-1}$; then

$$M_{t-1} \leq \frac{1}{z_t} E_t \sum_{s=t}^{\infty} z_s M_s \frac{R_s}{1+R_s}$$

• CB assets are not used to back money, money is "fiat"

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Fiat Money and CB Solvency

With fiat money and no interest on reserves, $S_t \ge 0$ can be ensured independently of portfolio trades

$$S_{t} = M_{t} - M_{t-1} + B_{t-1}^{B} + (1+Q_{t})D_{t-1}^{B} - \frac{B_{t}^{B}}{1+R_{t}} - Q_{t}D_{t}^{B}$$

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Fiat Money and CB Solvency

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An Equivalence Result

- Start from CE with CB buying long-term bonds
- New CE that respects bills only:
 - Set

$$\frac{\hat{B}_t^B}{1+R_t} = \frac{B_t^B}{1+R_t} + Q_t D_t^B$$

Set

$$\begin{split} \hat{S}_{t+1} = & S_{t+1} + [Q_t(1+R_t) - (1+Q_{t+1})]D_t^{\mathcal{B}} = \\ & S_{t+1} + \left(\beta_t E_t \left[(1+R_{t+1}) \frac{P_t}{P_{t+1}} \right] - 1 \right) Q_{t+1} D_t^{\mathcal{B}} \end{split}$$

• Adjust B_t , D_t so that $B_t - B_t^B$ and $D_t - D_t^B$ is unaffected

- New CE has same price system, allocation, same private holdings by maturity
- CB profits always positive, fiscal risk borne by Treasury

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4. Interest on Reserves

Strategy:

- Interest is paid on reserves (so X_t > 0 is possible);
- Proceeds may be invested in long-term securities Implications:
 - Leveraged bet on interest rate movements
 - Value of portfolio side can turn negative:

$$B_{t-1}^B + (1+Q_t)D_{t-1}^B - X_{t-1}$$

• CB can take unbounded fiscal risk

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Zero Interest Rates

- At zero interest rates, $X_t > 0$, arbitrarily high risks can be run
- But if no IOR is allowed, fiscal loss immediately recognized on exit (must liquidate portfolio)
- Early warning system
- Also, under bills only, still guaranteed positive profits

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Conclusion

- CB portfolio management causes fiscal risk
- Fiscal risk is unbounded with IOR
- QE can be equally well performed by Treasury by managing maturity structure
- Common instrument, conflicting objectives