

# Bringing Fiscal Policy into Monetary Policy

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## Motivation

- So far, we always neglected the transversality condition
- The government budget constraint did not play much of a role either
- Time for them to take center stage

## The household present-value budget constraint (PVBC): Start from periods 0 and 1...

- Period 0:

$$W_0 = M_0 + \frac{B_0}{1 + R_0} + E_0(z_{0,1}A_1)$$

- Period 1 (after multiplying by  $z_{0,1}$  and taking expected value as of period 0):

$$\begin{aligned} & E_0 [z_{0,1} (B_0 + M_0 + P(y_0 - c_{10} - c_{20}) + A_1 - T_1)] \\ = & E_0 [z_{0,1} W_1] = E_0 \left[ z_{0,1} \left( \frac{B_1}{1 + R_1} + M_1 + z_{1,2} A_2 \right) \right] \end{aligned}$$



## Combine periods 0 and 1

Substitute for  $E_0(z_1 A_1)$ :

$$W_0 = M_0(1 - E_0 z_{0,1}) + B_0 \left( \frac{1}{1 + R_0} - E_0 z_{0,1} \right) + E_0 \left[ z_{0,1} \left( P(c_{10} + c_{20} - y_0) + T_1 + \frac{B_1}{1 + R_1} + M_1 + z_{1,2} A_2 \right) \right]$$

Note: no-arbitrage requires  $\frac{1}{1+R_t} = E_t z_{t,t+1}$  So,

$$W_0 = M_0 \frac{R_0}{1 + R_0} + E_0 \left[ z_{0,1} \left( P(c_{10} + c_{20} - y_0) + T_1 + \frac{B_1}{1 + R_1} + M_1 + z_{1,2} A_2 \right) \right]$$

... on to periods up to  $J + 1$ ...

$$\begin{aligned}
 W_0 &= \sum_{s=0}^J E_0 z_{0,s} \frac{R_s}{1 + R_s} M_s + \sum_{s=0}^J E_0 [z_{0,s+1} (T_{s+1} - P_s(y_s - c_{1s} - c_{2s}))] \\
 &+ E_0 [z_{0,J+1} \left( \frac{B_{J+1}}{1 + R_{J+1}} + M_{J+1} + z_{J+1,J+2} A_{J+2} \right)] \\
 &= \sum_{s=0}^J E_0 z_{0,s} \frac{R_s}{1 + R_s} M_s + \sum_{s=0}^J E_0 [z_{0,s+1} (T_{s+1} - P_s(y_s - c_{1s} - c_{2s}))] \\
 &+ E_0 [z_{0,J+1} W_{J+1}]
 \end{aligned}$$

## ... and to infinity

Use no-Ponzi to replace  $E_0[z_{0,J+1}W_{J+1}]$  and take limit as  $J \rightarrow \infty$ :

- $$E_0[z_{0,J+1}W_{J+1}] \geq -E_0\left[\sum_{s=J+1}^{\infty} z_{0,s+1}(P_s y_s - T_{s+1})\right]$$
- $$W_0 \geq \sum_{s=0}^J E_0 z_{0,s} \frac{R_s}{1+R_s} M_s + \sum_{s=0}^{\infty} E_0 [z_{0,s+1} (T_{s+1} - P_s y_s)]$$

$$+ \sum_{s=0}^J E_0 [z_{0,s+1} p_s (c_{1s} + c_{2s})]$$
- $$W_0 \geq \frac{R_0}{1+R_0} M_0 + \sum_{s=0}^{\infty} E_0 [z_{0,s+1} (T_{s+1} - P_s y_s)]$$

$$+ \sum_{s=0}^{\infty} E_0 \left[ z_{0,s+1} \left( p_s (c_{1s} + c_{2s}) + \frac{R_{s+1}}{1+R_{s+1}} M_{s+1} \right) \right]$$

## Towards a government PVBC

- Repeat same steps on the government side
- Very similar, what is asset for household is liability for gov't
- No output, consumption (gov't does not trade in goods)
- Period 0 (note initial position of gov't is opposite of households, so the government owes  $W_0$ )

$$W_0 = M_0^S + \frac{B_0^S}{1 + R_0} = M_0^S + B_0 E_0 z_{0,1}$$

- Period 1 (after multiplying by  $z_{0,1}$  and taking exp value as of period 0)

$$E_0[z_{0,1}(B_0^S + M_0^S - T_1)] = E_0 \left[ z_{0,1} \left( z_{1,2} B_1^S + M_1^S \right) \right]$$

## Combine periods

- Combine with period 1:

$$W_0 = M_0^S \frac{R_0}{1 + R_0} + E_0 \left[ z_{0,1} \left( T_1 + \frac{B_1^S}{1 + R_1} + M_1^S \right) \right]$$

- On to periods up to  $J + 1$ :

$$W_0 = \sum_{s=0}^J E_0 z_{0,s} \frac{R_s}{1 + R_s} M_s^S + \sum_{s=0}^J E_0 z_{0,s+1} T_{s+1} + E_0 [z_{0,J+1} \left( \frac{B_{J+1}^S}{1 + R_{J+1}} + M_{J+1}^S \right)]$$

- Does gov't have a transversality condition?



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- Does gov't have a transversality condition?
- Does gov't have a no-Ponzi condition?

## Gov't PVBC

If we could say  $\lim_{J \rightarrow \infty} E_0[z_{0,J+1}(B_{J+1}^S/(1 + R_{J+1}) + M_{J+1}^S)] = 0$ ,  
then get Gov't PVBC

$$W_0 = \frac{R_0}{1 + R_0} M_0^S + \sum_{s=0}^{\infty} E_0 \left[ z_{0,s+1} \left( T_{s+1} + \frac{R_{s+1}}{1 + R_{s+1}} M_{s+1}^S \right) \right]$$

Seigniorage (inflation tax):

$$\frac{R_0}{1 + R_0} M_0^S + \sum_{s=0}^{\infty} E_0 \left[ z_{0,s+1} \frac{R_{s+1}}{1 + R_{s+1}} M_{s+1}^S \right]$$

Seigniorage are revenues that gov't cashes because money is an interest-free loan

## A different expression for seigniorage

$$\begin{aligned} \frac{R_0}{1 + R_0} M_0^S + \sum_{s=0}^{\infty} E_0 \left[ z_{0,s+1} \frac{R_{s+1}}{1 + R_{s+1}} M_{s+1}^S \right] &= \\ M_0^S (1 - E_0 z_{0,1}) + \sum_{s=0}^{\infty} E_0 \left[ z_{0,s+1} M_{s+1}^S (1 - z_{s+1,s+2}) \right] &= \\ M_0^S + \sum_{s=0}^{\infty} E_0 \left[ z_{0,s+1} (M_{s+1}^S - M_s^S) \right] \end{aligned}$$

- Seigniorage are revenues from printing money
- Notice: two definitions are equivalent ways of writing the same thing!

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- Suppose real bound is imposed on taxes
- Debt is still a promise to money  
Can gov't print unlimited quantities of money?



## The transversality condition under a money supply rule

- Under money supply rule, gov't cannot print unlimited money
- Then, taxes must adjust to meet budget constraint
- Limit on taxes  $\implies$  no-Ponzi condition, **at least for debt**:

$$\implies \lim_{J \rightarrow \infty} E_0[z_{0,J} B_J^S] = 0$$

- Our example tax policy satisfied this (we had  $B_t^S \equiv 0$ )
- There are many others that would work, but, given prices, gov't must meet obligations

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- There are many others that would work, but, given prices, gov't must meet obligations
- Even here, no need to back money with tax revenue

## The transversality condition under an interest-rate rule

- Under interest-rate rule, money supply infinitely elastic
- Gov't can meet debt obligations by printing money
- $\implies$  no-Ponzi constraint absent, transversality condition not imposed on gov't

## A first peek at CB independence

- Right now, we have only a consolidated gov't budget constraint
- Treasury can't print money to repay debt
- CB can (though usually done in a round-about way)
- Independent CB  $\implies$  Treasury may face limit

## One last important point

- $B_t^S$ : **nominal** debt
- no-Ponzi applies to **real** debt (denominated in gold, foreign currency)

## Does this matter?

- Households will exhaust their net worth, PVBC will hold as equality

$$\lim_{J \rightarrow \infty} E_0[z_{0,J+1} W_{J+1}] = 0$$

- Substitute market clearing:

$$\lim_{J \rightarrow \infty} E_0[z_{0,J+1} \left( \frac{B_{J+1}^S}{1 + R_{J+1}} + M_{J+1}^S \right)] = 0$$

- Voilà: transversality condition obtained, write PVBC:

$$W_0 = \frac{R_0}{1 + R_0} M_0^S + \sum_{s=0}^{\infty} E_0 \left[ z_{0,s+1} \left( T_{s+1} + \frac{R_{s+1}}{1 + R_{s+1}} M_{s+1}^S \right) \right]$$

## It does matter!

- Market clearing is an **equilibrium** condition
- Does not have to hold for all prices
- If gov't PVBC does not hold, what adjusts: prices or taxes?

## What adjusts?

- Money supply rule, real debt, independent CB: taxes
- Otherwise: maybe taxes, maybe prices
- When prices adjust, **fiscal theory of the price level (FTPL)**



## The FTPL with an interest rate peg

- We saw that setting a constant interest rate  $\bar{R}$  would deliver indeterminate  $P_0$  (and sunspots)
- Suppose now we set  $T_0$  fixed,  $T_t = \bar{T}P_{t-1}$  for some constant  $\bar{T}$ .
- Check transversality condition (or gov't PVBC): what prices are consistent with competitive equilibrium?

## Gov't PVBC under fixed real taxes - 1

- Need to check

$$W_0 = \frac{\bar{R}}{1 + \bar{R}} M_0 + \sum_{s=0}^{\infty} E_0 \left[ z_{0,s+1} \left( P_s \bar{T} + \frac{\bar{R}}{1 + \bar{R}} M_{s+1} \right) \right]$$

## Gov't PVBC under fixed real taxes - 1

- Need to check

$$W_0 = \frac{\bar{R}}{1 + \bar{R}} M_0 + \sum_{s=0}^{\infty} E_0 \left[ z_{0,s+1} \left( P_s \bar{T} + \frac{\bar{R}}{1 + \bar{R}} M_{s+1} \right) \right]$$

- Use CIA, Friedman distortion:

$$M_s = P_s c_{1s} = P_s \bar{c}, \text{ where } \bar{c} := (u')^{-1}(1 + \bar{R})$$

- Need to check

$$W_0 = \frac{P_0 \bar{c} \bar{R}}{1 + \bar{R}} + \sum_{s=0}^{\infty} E_0 [z_{0,s+1} P_s \bar{T}] + \frac{\bar{c} \bar{R}}{1 + \bar{R}} \sum_{s=0}^{\infty} E_0 [z_{0,s+1} P_{s+1}]$$

## Gov't PVBC under fixed real taxes - 2

From CE conditions

- $\lambda_t P_t = u'(c_{1t}) = u'(\bar{c})$
- $z_{t,t+1} P_{t+1} = \beta \lambda_{t+1} P_{t+1} / \lambda_t = \beta P_t$  (note no expectation)
- Recursively,  $z_{0,t+1} P_{t+1} = \beta^{t+1} P_0$  (also,  
 $E_0(z_{s,s+1}) = 1/(1 + \bar{R})$ )

Substitute, need to check

$$W_0 = \frac{P_0}{(1 - \beta)(1 + \bar{R})} [\bar{c}\bar{R} + \bar{T}]$$

## The FTPL in action

- Equation to check:

$$W_0 = \frac{P_0}{(1 - \beta)(1 + \bar{R})} [\bar{c}\bar{R} + \bar{T}]$$

- $W_0$  given (initial condition)
- $\bar{T}, \bar{R}$  given,  $\bar{c}$  determined by  $\bar{R}$
- $\implies$  at most **one**  $P_0$  will work!
- Solution exists if  $\text{sign}(W_0) = \text{sign}(\bar{T} + \bar{R}\bar{c})$

## Economic intuition on the FTPL

- Initial **nominal** government liabilities:  $W_0$
- Gov't PVBC: PV of gov't surpluses = liabilities
- Given fiscal policy, PV of taxes fixed **real** amount
- Seigniorage ( $\bar{R}\bar{c}$ ) also fixed **real** amount
- Price level must be the ratio of nominal liabilities to real surpluses

## More economic intuition on the FTPL

- Under the FTPL, bonds are claims to money
- Money (and thus bonds) is an entitlement to tax revenues, cannot be worthless
- Suppose  $P_0$  above equilibrium level and  $W_0 > 0$
- Gov't has excess resources  $\implies$  households do not have enough wealth to support their consumption
- $\implies$  households cut back on their consumption
- Excess supply  $\implies$  prices go down, until equilibrium attains

## Why intuition in previous slide is loose

- Previous slide describes a process by which the equilibrium is attained
- But this is really a mental process
- The economy is **always** in equilibrium
- “Starting from  $P_0$  low” is a thought experiment, we do not model this



## The FTPL and sunspots

- Without FTPL, under a fixed interest rate peg, we got lots of sunspot equilibria
- Sunspot equilibrium: inflation can be random
- Just as FTPL pins down  $P_0$ , it kills all sunspots as well (repeat algebra from period 1)

## The FTPL and CB independence

- FTPL is the **only** complete theory of what pins down the price level
- Unpleasant feature: it's not CB, it's Treasury that matters!!

## The effect of uncertainty and fiscal news: before the news breaks

- Introduce uncertainty in a single period,  

$$T_{T+1} = P_T(\bar{T} + \tilde{T}_{T+1})$$
- $\tilde{T}_{T+1}$  revealed at time  $t < T + 1$ , and  $E_s \tilde{T}_{T+1} = 0$  for  $s < t$
- Note: similar logic when  $t = T + 1$ , but equations a bit more involved because jump in taxes and jump in prices occur at the same time  $\implies$  jump in real taxes depends on jump in prices

## Period 0

- We still get

$$W_0 = \frac{R_0}{1 + R_0} M_0^S + \sum_{s=0}^{\infty} E_0 \left[ z_{0,t+1} \left( T_{t+1} + \frac{R_{t+1}}{1 + R_{t+1}} M_{t+1}^S \right) \right]$$

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$$W_0 = \frac{P_0 \bar{c} \bar{R}}{1 + \bar{R}} + \sum_{t=0}^{\infty} E_0 [z_{0,t+1} P_t T_{t+1}] + \frac{\bar{c} \bar{R}}{1 + \bar{R}} \sum_{t=0}^{\infty} E_0 [z_{0,t+1} P_{t+1}]$$

- Risk neutrality crucial here ( $z_{0,t+1} P_{t+1} = \beta^t P_0$ )

$$W_0 = \frac{P_0 \bar{c} \bar{R}}{(1 + \bar{R})(1 - \beta)} + P_0 \sum_{t=0}^{\infty} \beta^t E_0 [T_{t+1}] = \frac{P_0 (\bar{c} \bar{R} + \bar{T})}{(1 - \beta)(1 + \bar{R})}$$

- Without risk neutrality, fiscal risk would have an effect on expected values

## Subsequent periods

- Can verify that the PVBC holds for all periods  $s \geq 0$ :

$$W_s = \frac{R_s}{1 + R_s} M_s^S + \sum_{v=s}^{\infty} E_s \left[ z_{s,v+1} \left( T_{v+1} + \frac{R_{v+1}}{1 + R_{v+1}} M_{v+1}^S \right) \right]$$

- But also (flow bc + mkt clearing)

$$W_{s+1} = W_s(1 + R_s) - T_{s+1} - R_s M_s$$

## Periods $0 < s < t$

- 

$$E_s T_v = \bar{T} \quad s \leq v, \quad s < t$$

- From PVBC

$$W_s = \frac{P_s}{(1 - \beta)(1 + \bar{R})} [\bar{c}\bar{R} + \bar{T}]$$

- From flow BC (and PV as of  $s - 1$ )

$$W_s = W_{s-1}(1 + \bar{R}) - P_{s-1}(\bar{T} + \bar{c}\bar{R}) = \frac{P_{s-1}\beta}{1 - \beta} [\bar{c}\bar{R} + \bar{T}]$$

- Get  $P_s = \beta P_{s-1} / (1 + \bar{R})$

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- Get  $P_s = \beta P_{s-1} / (1 + \bar{R})$
- Same as Euler equation, but no uncertainty (sunspots not possible; here risk neutrality not important, just no news)

## Period $t$

- 

$$E_t T_v = \bar{T} \quad v \neq T+1, \quad E_t T_{T+1} = \bar{T} + \check{T}_{T+1}$$

- From PVBC

$$W_t = \frac{P_t}{(1-\beta)(1+\bar{R})} [\bar{c}\bar{R} + \bar{T}] + \frac{\beta^{T-t} \check{T}_{T+1} P_t}{1+\bar{R}}$$

- From flow BC (and PV as of  $t-1$ )

$$W_t = \frac{P_{t-1} \beta}{1-\beta} [\bar{c}\bar{R} + \bar{T}]$$

- Get

$$\frac{1}{P_t} = \frac{1}{P_{t-1}} \left[ \frac{1}{\beta(1+\bar{R})} + \frac{\beta^{T-t}(1-\beta)\check{T}_{T+1}}{\beta(1+\bar{R})(\bar{T} + \bar{c}\bar{R})} \right]$$

- Euler holds (expected value as of  $t-1$ ), still no sunspots, price jumps on fiscal news



Period  $s \geq t + 1$

- Homework
- Verify that  $P_s = \beta P_{s-1} / (1 + \bar{R})$
- No uncertainty again, no sunspots

## Patching up CB independence

- Is that a death knell for CB independence?

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- Is that a death knell for CB independence?
- CB retains control of inflation after time 0 (it is deterministic and equal to  $\beta(1 + \bar{R})$ )
- Also, no more pesky sunspots

## Combining local determinacy with FTPL

- Start from an active Taylor rule ( $\alpha > 1$ )
- Add a fiscal policy that prunes equilibria with very high or very low inflation
- On a day-to-day basis inflation responds the way it would in the locally-unique equilibrium

## Active and Passive Monetary Policy Rules

- Recall Taylor principle for interest-rate rules:
  - $\alpha > 1$ : strong response to inflation, Fisher equation is a divergent difference equation (except for SS)
  - $\alpha < 1$ : weak response to inflation, Fisher equation is convergent
- When Fisher equation is divergent, we say that monetary policy is **active**
- When Fisher equation is convergent, we say that monetary policy is **passive**

## Active and Passive Fiscal Policy Rules

- Same “active” and “passive” language applies to fiscal policy rules, but what is the relevant difference equation?

## Active and Passive Fiscal Policy Rules

- Same “active” and “passive” language applies to fiscal policy rules, but what is the relevant difference equation?
- The gov't budget constraint!
- Define  $H_t := E_0 \left[ z_{0,t} \left( \frac{B_t^S}{1+R_t} + M_t^S \right) \right]$
- Get

$$H_t = H_{t-1} + E_0[M_{t-1}^S(z_{0,t} - z_{0,t-1})] - E_0[z_{0,t} T_t] =$$
$$H_{t-1} - E_0 \left[ \frac{z_{0,t-1} M_{t-1}^S R_{t-1}}{1 + R_{t-1}} \right] - E_0[z_{0,t} T_t] \quad (1)$$

## Initial condition

$$H_0 = \frac{B_0^S}{1 + R_0} + M_0^S = W_0$$





## Why do we write the budget constraint as in the previous slides?

Because it is the left-hand side that has to converge to 0 for PVBC to hold

## Example of a Passive Fiscal Policy Rule

- Passive fiscal policy rule = difference equation converges to 0 no matter what  $P_0$  is
- Technical assumption :  $\lim_{R \rightarrow \infty} R(u')^{-1}(1 + R) < \infty$
- $\implies$  implies  $R(u')^{-1}(1 + R) < \bar{S}$ , i.e., seigniorage revenues are bounded

$$T_t = \gamma(M_{t-1}^S + B_{t-1}^S)$$

With  $\gamma \in (0, 1)$ : taxes cover at least fraction  $\gamma$  of nominal liabilities

## Verifying that the previous rule is passive - 1

Substitute fiscal policy rule

$$\begin{aligned} H_t &= H_{t-1} - E_0 \left[ z_{0,t-1} \left( \frac{M_{t-1}^S R_{t-1}}{1 + R_{t-1}} + \gamma \frac{M_{t-1}^S + B_{t-1}^S}{1 + R_{t-1}} \right) \right] \\ &= (1 - \gamma) H_{t-1} - (1 - \gamma) E_0 \left[ z_{0,t-1} \frac{M_{t-1}^S R_{t-1}}{1 + R_{t-1}} \right], \quad t > 0 \end{aligned}$$

## Verifying that the previous rule is passive - 2

From competitive equilibrium

$$z_{0,t-1} = \frac{\beta^{t-1}(1 + R_{t-1})P_0}{P_{t-1}(1 + R_0)}$$

$$H_t = (1 - \gamma) \left( H_{t-1} - (1 + R_0)^{-1} \beta^{t-1} \frac{R_{t-1} M_{t-1}^S P_0}{P_{t-1}} \right), \quad t > 0$$

Use Friedman distortion, CIA if  $R_t > 0$ , and technical assumption:

$$|H_t| \leq (1 - \gamma)|H_{t-1}| + (1 - \gamma)\beta^{t-1}(1 + R_0)^{-1}P_0\bar{S}, \quad t > 0$$

## Verifying that the previous rule is passive - 3

$$\begin{aligned}
 |H_t| &\leq (1 - \gamma)^t |H_0| + (1 + R_0)^{-1} P_0 \bar{S} \sum_{s=0}^{t-1} \beta^s (1 - \gamma)^{t-s} = \\
 (1 - \gamma)^t &\left[ |H_0| + \frac{(1 + R_0)^{-1} P_0 \bar{S} \left( 1 - \left( \frac{\beta}{1 - \gamma} \right)^t \right)}{1 - \frac{\beta}{1 - \gamma}} \right] = \\
 (1 - \gamma)^t &\left[ |H_0| + \frac{(1 + R_0)^{-1} P_0 \bar{S}}{1 - \frac{\beta}{1 - \gamma}} \right] - \frac{\beta^t (1 + R_0)^{-1} P_0 \bar{S}}{1 - \frac{\beta}{1 - \gamma}} \rightarrow_{t \rightarrow \infty} 0.
 \end{aligned}$$

## Active Fiscal Policy Rule

- Active fiscal policy rule = difference equation does not converge to 0, except for one value of  $P_0$
- Example:  $T_t = \bar{T}P_{t-1}$  (with  $R_t = \bar{R}$ )

## A Difference between Exploding Paths

- Paths where inflation explodes according to

$$(\log \pi_{t+1} - \log \bar{\pi}) = \alpha(\log \pi_t - \log \bar{\pi})$$

are not ruled out by any equilibrium conditions

- Paths where debt explodes according to

$$H_t = H_{t-1} = H_{t-1} - E_0 \left[ \frac{z_{0,t-1} M_{t-1}^S R_{t-1}}{1 + R_{t-1}} \right] - E_0[z_{0,t} T_t]$$

violate the households' transversality condition, ruled out by equilibrium

## A Weaker Notion of Active Fiscal Policy

- Compute equilibrium difference equation for  $W_t/P_t$
- Fiscal policy active if the difference equation is explosive
- Adopted by Bianchi, Melosi and coauthors, sometimes Leeper and coauthors,...
- Rationale: equilibria with exploding household wealth are weird...
- ... but they are still equilibria, unless the explosion is sufficiently fast to violate transversality



## A Final Classification

	Fiscal Policy	
	Passive	Active (strong sense)
Interest-rate rule: Passive	Indeterminacy	Uniqueness
Interest-rate rule: Active	Local uniqueness	Uniqueness, explosive